## MATHEMATICS-II

Subject Code : MA201BS<br>Regulations : R18-JNTUH<br>Class : I Year B.Tech II Semester



Department of Science and Humanities

BHARAT INSTITUTE OF ENGINEERING AND TECHNOLOGY

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## MATHEMATICS-II (MA201BS)

## COURSE PLANNER (2018-19)

## I. COURSE OVERVIEW:

The students will improve their ability to think critically, to analyze a real problem and solve it using a wide array of mathematical tools. They will also be able to apply these ideas to a wide range of problems that include the Engineering applications.

## II. PREREQUISITE:

1. Basic knowledge of Differentiation.
2. Basic knowledge of Integration.
3. Basic knowledge of calculation of basic formulas.
4. Basic knowledge of partial differentiation.
III. COURSE OBJECTIVE: To learn

| 1. | Methods of solving the differential equations of first and higher order. |
| :--- | :--- |
| 2. | Evaluation of multiple integrals and their applications. |
| 3. | The physical quantities involved in engineering field related to vector valued functions. |
| 4. | The basic properties of vector valued functions and their applications to line, surface and <br> volume integrals. |

IV.COURSE OUTCOMES: After learning the contents of this paper the student must be able to

| S. No | Description | Bloom's Taxonomy Level |
| :---: | :--- | :---: |
| 1. | Identify whether the given differential <br> equation of first order is exact or not. | Understand, Apply <br> (Level 2, Level 3) |
| 2. | Solve higher differential equation and apply <br> the concept of differential equation to real <br> world problems. | Understand, Apply <br> (Level 2, Level 3) |
| 3. | Evaluate the multiple integrals and apply the <br> concept to find areas, volumes, centre of mass <br> and Gravity for cubes, sphere and rectangular <br> parallelepiped. | Understand, Apply <br> (Level 2, Level 3) |
| 4. | Evaluate the line, surface and volume <br> integrals and converting them from one to <br> another . | Understand, Apply <br> (Level 2, Level 3) |
| 5 | Apply Gauss, Greens and Stokes theorems <br> Understand, Apply <br> (Level 2, Level 3) |  |

## V. HOW PROGRAM OUTCOMES ARE ASSESSED:

|  | Program Outcomes | Level | Proficiency Assessed by |
| :---: | :---: | :---: | :---: |
| PO1 | Engineering knowledge: To Apply the knowledge of mathematics, science, engineering fundamentals, and Computer Science Engineering to the solution of complex engineering problems encountered in modern engineering practice. | 3 | Assignments and Tutorials. |
| PO2 | Problem analysis: Ability to Identify, formulate, review research literature, and analyze complex engineering problems related to Computer Science reaching substantiated conclusions using first principles of mathematics, natural sciences, and engineering sciences. | 2 | Assignments, Tutorials and Exams. |
| PO3 | Design/development of solutions: Design solutions for complex engineering problems and design system components or processes that meet the specified needs with appropriate consideration for the public health and safety, and the cultural, societal, and environmental considerations. | 2 | Assignments, Tutorials and Exams. |
| P04: | Conduct investigations of complex problems: Use researchbased knowledge and research methods including design of experiments, analysis and interpretation of data, and synthesis of the information to provide valid conclusions. | 1 | Assignments, Tutorials and Mock Exams. |
| P05: | Modern tool usage: Create, select, and apply appropriate techniques, resources, and modern Computer Science Engineering and IT tools including prediction and modeling to complex engineering activities with an understanding of the limitations. | - | -- |
| P06: | The engineer and society: Apply reasoning informed by the contextual knowledge to assess societal, health, safety, legal and cultural issues and the consequent responsibilities relevant to the Computer Science Engineering professional engineering | - | -- |
| P07: | Environment and sustainability: Understand the impact of Computer Science Engineering professional engineering solutions in societal and environmental contexts, and demonstrate the knowledge of, and need for sustainable development. | - | -- |
| P08: | Ethics: Apply ethical principles and commit to professional ethics and responsibilities and norms of the engineering practice. | - | -- |
| PO9: | Individual and team work: Function effectively as an individual, and as a member or leader in diverse teams, and in multidisciplinary settings. | - | -- |
| P010: | Communication: Communicate effectively on complex engineering activities with the engineering community and with society at large, such as, being able to comprehend and write | - | -- |
| PO11: | Project management and finance: Demonstrate knowledge and understanding of the engineering and management principles and apply these to one's own work, as a member and leader in a team, to manage projects and in multidisciplinary environments. | - | -- |
| P012: | Life-long learning: Recognize the need for, and have the preparation and ability to engage in independent and life-long learning in the broadest context of technological change. | - | -- |

1: Slight (Low) 2: Moderate (Medium) 3: Substantial (High) 4: None

## VI. HOW PROGRAM SPECIFIC OUTCOMES ARE ASSESSED:

| Program Specific Outcomes | Level | Proficiency <br> assessed by |  |
| :---: | :--- | :---: | :--- |
| PSO1 | Foundation of mathematical concepts: To use mathematical <br> methodologies to crack problem using suitable mathematical <br> analysis, data structure and suitable algorithm. | $\mathbf{2}$ | Assignments, <br> Tutorials and <br> Exams. |
| PSO2 | Foundation of Computer System: The ability to interpret the <br> fundamental concepts and methodology of computer systems. <br> Students can understand the functionality of hardware and <br> software aspects of computer systems. | $\mathbf{1}$ | Tutorials and Mock |
| Exams. |  |  |  |
| PSO3 | Foundations of Software development: The ability to grasp <br> the software development lifecycle and methodologies of <br> software systems. Possess competent skills and knowledge of <br> software design process. Familiarity and practical proficiency <br> with a broad area of programming concepts and provide new <br> ideas and innovations towards research. | $\mathbf{-}$ |  |

1: Slight (Low) 2: Moderate (Medium) 3: Substantial (High) 4: None

## VII. SYLLABUS:

## UNIT-I: First Order ODE

Exact, linear and Bernoulli's equations; Applications: Newton's law of cooling, Law of natural growth and decay; Equations not of first degree: equations solvable for p , equations solvable for y , equations solvable for x and Clairaut's type

## UNIT-II: Ordinary Differential Equations of Higher Order

Second order linear differential equations with constant coefficients: Non-Homogeneous terms of the type $\mathrm{e}^{\mathrm{ax}}, \sin a \mathrm{x}, \cos a \mathrm{x}$, polynomials in $x, \mathrm{e}^{\mathrm{ax}} V(x)$ and $x V(x)$; method of variation of parameters; Equations reducible to linear ODE with constant coefficients: Legendre's equation, Cauchy-Euler equation.

## UNIT-III: Multivariable Calculus (Integration)

Evaluation of Double Integrals (Cartesian and polar coordinates); change of order of integration (only Cartesian form); Evaluation of Triple Integrals: Change of variables (Cartesian to polar) for double and (Cartesian to Spherical and Cylindrical polar coordinates) for triple integrals. Applications: Areas (by double integrals) and volumes (by double integrals and triple integrals), Centre of mass and Gravity (constant and variable densities) by double and triple integrals (applications involving cubes, sphere and rectangular parallelopiped).

## UNIT-IV: Vector Differentiation

Vector point functions and scalar point functions. Gradient, Divergence and Curl. Directional derivatives, Tangent plane and normal line. Vector Identities. Scalar potential functions. Solenoidal and Irrotational vectors.

## UNIT-V: Vector Integration

Line, Surface and Volume Integrals. Theorems of Green, Gauss and Stokes (without proofs) and their applications.

## GATE SYLLABUS:

Differential Equations: Ordinary Differential Equations First order ordinary differential equations, existence and uniqueness theorems for initial value problems, systems of linear first order ordinary differential equations, linear ordinary differential equations of higher order with constant coefficients; linear second order ordinary differential equations with variable coefficients

## Linear Systems of Equations:

Linear transformations and their matrix representations, rank; systems of linear equations, Hermitian, Skew Hermitian and unitary matrices, Jordan

## Eigen values, Eigen Vectors:

Eigen values and eigenvectors, minimal polynomial, Cayley-Hamilton Theorem, diagonalization

Functions of several variables: Functions of several variables, maxima, minima

## Partial Differential Equations:

Partial Differential Equations Linear and quasi-linear first order partial differential equations, method of characteristics; second order linear equations in two variables and their classification;

## IES SYLLABUS:

Matrix: Matrix theory, Eigen values \& Eigen vectors, system of linear equations

Differential Equations: Numerical methods for solution of non-linear algebraic equations and differential equations

Partial differential equations: Partial derivatives, linear, nonlinear and partial differential equations, initial and boundary value problems.

## VIII. LESSON PLAN-COURSE SCHEDULE:

|  |  | $\stackrel{\text { 兑 }}{ }$ | TOPIC | Course learning outcomes | Reference |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1. | 1 | 1 | Introduction to differential equations | Define DE and PDE | T1,T2,R2 |
| 2. |  |  | Linear differential equation | Solve problems on linear | T1,T2,R2 |
| 3. |  |  | Bernoulli's differential equation | Solve problems on bernoullis | T1,T2,R2 |
| 4. |  |  | Exact differential equation | Solve problems on exact | T1,T2,R2 |
| 5. | 2 |  | Applications of differential equation | Understand applications | T1,T2,R2 |
| 6. |  |  | Newton's law of cooling | Solve problems on law of cooling | T1,T2,R2 |
| 7. |  |  | Law of natural growth and decay | Solve problems on natural | T1,T2,R2 |


|  |  |  |  | growth |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 8. | 3 |  | Law of natural growth and decay | Solve problems on natural decay | T1,T2,R2 |
| 9. |  |  | Equations not of first degree | Solve problems on equations not of first degree | T1,T2,R2 |
| 10. |  |  | Equations solvable for p | Solve problems on equations solvable for p | T1,T2,R2 |
| 11. |  |  | equations solvable for y and x | Solve problems on equations solvable for $\mathrm{x}, \mathrm{y}$ | T1,T2,R2 |
| 12. |  |  | Clairaut's type | Solve problems on clairauts | T1,T2,R2 |
|  |  |  | *Applications of Electrical Circuits (content beyond syllabus) | Understand applications |  |
|  |  |  | Mock Test - I |  |  |
| UNIT - 2 |  |  |  |  |  |
| 13. | 4 | 2 | Second order <br> equations linear <br> with differential <br> coefficients <br>    | Find second order linear DE | T1,T2,R2 |
| 14. |  |  | Non-Homogeneous terms of the type $\mathrm{e}^{\text {ax }}$ | Solve problems of type $\mathrm{e}^{\text {ax }}$ | T1,T2,R2 |
| 15. | 5 |  | Non-Homogeneous terms of the type $\sin a x$ | Solve problems of type sinax | T1,T2,R2 |
| 16. |  |  | Non-Homogeneous terms of the type cosax | Solve problems of type cosax | T1,T2,R2 |
| 17. |  |  | Non-Homogeneous terms of the type polynomials in $x$ | Solve problems of type x | T1,T2,R2 |
| 18 |  |  | Non-Homogeneous terms of the type $\mathrm{e}^{\mathrm{ax}} V(x)$ | Solve problems of type $\mathrm{e}^{\mathrm{ax}} V(x)$ | T1,T2,R2 |
| 19 |  |  | Non-Homogeneous terms of the type $x V(x)$ | Solve problems of type $x V(x)$ | T1,T2,R2 |
| 20. |  |  | method of variation of parameters | Solve problems using variation of parameters | T1,T2,R2 |
| 21. | 6 |  | Equations reducible to linear ODE with constant coefficients | Find equations reducible to linear | T1,T2,R2 |
| 22. |  |  | Equations reducible to linear ODE with constant coefficients | Find equations reducible to linear | T1,T2,R2 |
| 23. |  | 2 | Legendre's equation | Solve problems on legendres | T1,T2,R2 |
| 24. |  |  | Cauchy-Euler equation. | Solve problems on cauchys euler equation | T1,T2,R2 |
|  |  |  | * Applications of Simple <br> Harmonic <br> Motions content | Understand applications |  |


|  |  |  | beyond syllabus) |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Tutorial / Bridge Class \# 1 |  |  |
| UNIT - 3 |  |  |  |  |  |
| 25. | 7 | 3 | Evaluation of Double Integrals (Cartesian and polar coordinates) | Apply double integrals | T2,R3,R1 |
| 26. |  |  | Evaluation of Double Integrals (Cartesian and polar coordinates) | Apply double integrals | T2,R3,R1 |
| 27. |  |  | Evaluation of Triple Integrals | Apply triple integrals | T2,R3,R1 |
| 28. |  |  | Evaluation of Triple Integrals | Apply triple integrals | T2,R3,R1 |
| 29. | 8 |  | Applications: Areas (by double integrals) | Find areas using double integration | T2,R3,R1 |
| 30. |  |  | Applications: Areas (by double integrals) | Find areas using double integration | T2,R3,R1 |
| 31. |  |  | Applications: volumes (by double integrals and triple integrals) | Find volume using triple integration | T2,R3,R1 |
| 32. |  |  | Applications: volumes (by double integrals and triple integrals) | Find volume using triple integration | T2,R3,R1 |
|  |  |  | Tutorial / Bridge Class \# 2 |  |  |
| I Mid Examinations |  |  |  |  |  |
| 33. | 9 | 3 | change of order of integration (only Cartesian form) | Apply change of order | T2,R3,R1 |
| 34. |  |  | Change of variables (Cartesian to polar) for double and (Cartesian to Spherical and Cylindrical polar coordinates) for triple integrals | Apply change of variable | T2,R3,R1 |
| 35. |  |  | Centre of mass and Gravity (constant and variable densities) by double and triple integrals (applications involving cubes, sphere and rectangular parallelopiped). | Find centre of mass and gravity | T2,R3,R1 |
| 36. |  |  | Centre of mass and Gravity (constant and variable densities) by double and triple integrals (applications involving cubes, sphere and rectangular parallelopiped). | Find centre of mass and gravity | T2,R3,R1 |
|  |  |  | - Evaluation of surface and volume using MATLAB (contents beyond the syllabus) | Understand application |  |
| UNIT - 4 |  |  |  |  |  |
| 37 | 10 |  | Vector point functions | Define vector point function | T1,T3, R1,R2 |
| 38 |  |  | scalar point functions | Define scalar point function | T1,T3, R1,R2 |


| 39 |  | 4 | Gradient | Apply Gradient | T1,T3, R1,R2 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 40 |  |  | Divergence | Find Divergence | T1,T3, R1,R2 |
| 41 | 11 |  | Directional derivatives | Find directional derivatives | T1,T3, R1,R2 |
| 42 |  |  | Curl | Find Curl | T1,T3, R1,R2 |
| 43 |  |  | Tangent plane and normal line | Find tangent and normal plane | T1,T3, R1,R2 |
| 44 |  |  | Vector Identities | Apply vector identities | T1,T3, R1,R2 |
|  |  |  | Tutorial / Bridge Class \# 3 |  |  |
| 45 | 12 |  | Vector Identities | Apply vector identities | T1,T3, R1,R2 |
| 46 |  |  | Scalar potential functions | Find scalar potential function | T1,T3, R1,R2 |
| 47 |  |  | Solenoidal vectors | Find solenoidal vector | T1,T3, R1,R2 |
| 48 |  |  | Irrotational vectors | Find irrotational vectors | T1,T3, R1,R2 |
|  |  |  | Applications of improper integrals and Signals and Systems(content beyond the syllabus) | Understand application |  |
|  |  |  | Mock Test - II |  |  |
| UNIT - 5 |  |  |  |  |  |
| 49 | 13 | 5 | Line integral | Evaluate Line integral | T1,T3, R1,R2 |
| 50 |  |  | Line integral | Evaluate Line integral | T1,T3, R1,R2 |
| 51 |  |  | Surface integral | Evaluate surface integral | T1,T3, R1,R2 |
| 52 |  |  | Surface integral | Evaluate surface integral | T1,T3, R1,R2 |
| 53 | 14 |  | Volume integral | Evaluate volume integral | T1,T3, R1,R2 |
| 54 |  |  | Volume integral | Evaluate volume integral | T1,T3, R1,R2 |
| 55 |  |  | Gauss Divergence Theorem | Apply gauss theorem | T1,T3, R1,R2 |
| 56 |  |  | Gauss Divergence Theorem | Apply gauss theorem | T1,T3, R1,R2 |
| 57 | 15 |  | Greens Theorem | Apply greens theorem | T1,T3, R1,R2 |
| 58 |  |  | Greens Theorem | Apply greens theorem | T1,T3, R1,R2 |
| 59 |  |  | Stokes Theorem | Apply stokes theorem | T1,T3, R1,R2 |
| 60 |  |  | Stokes Theorem | Apply stokes theorem | T1,T3, R1,R2 |
|  |  |  | PDE applications in Computational Fluid Dynamics and Aerodynamics etc.(content beyond syllabus) | Understand application |  |
|  |  |  | Tutorial / Bridge Class \# 4 |  |  |
| II Mid Examinations |  |  |  |  |  |

## SUGGESTED BOOKS:

## TEXT BOOKS:

1. B.S. Grewal, Higher Engineering Mathematics, Khanna Publishers, 36th Edition, 2010
2. Erwin kreyszig, Advanced Engineering Mathematics, $9_{\text {th }}$ Edition, John Wiley \& Sons, 2006 3. G.B. Thomas and R.L. Finney, Calculus and Analytic geometry, 9thEdition, Pearson, Reprint, 2002.

## REFERENCES:

1. Paras Ram, Engineering Mathematics, 2nd Edition, CBS Publishes
2. S. L. Ross, Differential Equations, 3rd Ed., Wiley India, 1984.

## IX. MAPPING COURSE OUTCOMES LEADING TO THE ACHIEVEMENT OF PROGRAM OUTCOMES AND PROGRAM SPECIFIC OUTCOMES:

| Oٍ | Program Outcomes (PO) |  |  |  |  |  |  |  |  |  |  |  | Program Specific Outcomes (PSO) |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | PO1 | PO2 | PO3 | PO4 | PO5 | PO6 | PO7 | PO8 | P09 | PO10 | P011 | $\begin{gathered} \text { PO } \\ 12 \end{gathered}$ | PSO1 | PSO2 | PSO3 |
| I | 3 | 2 | 2 | 1 | - | - | - | - | - | - | - | - | 2 | 1 | - |
| II | 2 | 2 | 2 | 1 | - | - | - | - | - | - | - | - | 1 | 1 | - |
| III | 3 | 1 | 2 | 1 | - | - | - | - | - | - | - | - | 2 | 1 | - |
| IV | 3 | 2 | 1 | 1 | - | - | - | - | - | - | - | - | 2 | 1 | - |
| V | 2 | 2 | 2 | 1 | - | - | - | - | - | - | - | - | 1 | 1 | - |
| AVG | 2.6 | 1.8 | 1.8 | 1.0 | - | - | - | - | - | - | - | - | 1.6 | 1.0 | - |
| 1: Slight(Low) |  |  |  | 2: Moderate (Medium) |  |  |  |  |  | 3: Substantial(High) |  |  | 4 : None |  |  |

## QUESTION BANK: (JNTUH)

## DESCRIPTIVE QUESTIONS:

## UNIT I

## Short Answer Questions

| S.No | Question | Blooms <br> taxonomy <br> level | Course <br> outcome |
| :---: | :--- | :--- | :---: |
| 1 | Solve $\left(e^{y}+1\right) \cos x d x+e^{y} \sin x d y=0$ | Understand | 1 |
| 2 | Solve $\left(1+e^{x / y}\right) d x+e^{x / y}(1-\mathrm{x} / \mathrm{y}) \mathrm{dy}=0$. | Understand | 1 |
| 3 | Solve the differential equation $(\mathrm{y}-\mathrm{yx}) \mathrm{dx}+(\mathrm{x}+\mathrm{xy}) \mathrm{dy}=0$. | Understand | 1 |
| 4 | Write the working rule to solve Bernoulli's equation. | Remember | 1 |
| 5 | A copper ball is heated to a temperature of 80 c if at time $\mathrm{t}=0$ in <br> water which is maintained at 30C. If at $\mathrm{t}=3$ minutes, the temperature <br> of the ball is reduced to 50C. Find the time at which the temperature <br> of the ball is 40C. | Apply | 1 |
| 6 | Sovle the differential equation $x^{2} y d x-\left(x^{3}+y^{3}\right) d y=0$ | Understand | 1 |
| 7 | Solve $(\mathrm{xy} \operatorname{Sin} \mathrm{xy}+\operatorname{Cos} \mathrm{Cy}) \mathrm{y} \mathrm{dx}+(\mathrm{xy} \sin \mathrm{xy}-\operatorname{Cos} \mathrm{xy}) \mathrm{x}$ dy $=0$ | Understand | 1 |

\(\left.\begin{array}{|c|l|c|c|}\hline 8 \& Solve the differential equation \frac{d y}{d x}+y \tan x=y^{2} \sec x \& Understand \& 1 <br>
\hline 9 \& \begin{array}{l}If the air is maintained at 25^{\circ} \mathrm{C} and temperature of the body cools <br>
from 140^{\circ} \mathrm{C} to 80^{\circ} \mathrm{C} in 20 minutes find when the temperature will <br>

be 35^{\circ} \mathrm{C} .\end{array} \& Apply\end{array}\right]\)| 1 |
| :---: |
| 10 | Solve the differential equation $y\left(2 x y+e^{x}\right) d x-e^{x} d y=0 \quad$ Understand | 1 |
| :--- |

## Long Answer Questions

| S.No | Question | Blooms <br> taxonomy <br> level | Course <br> outcome |
| :---: | :--- | :--- | :---: |
| 1 | Solve the differential equation $\frac{d y}{d x}+y \tan x=y^{2} \sec x$ | Understand | 1 |
| 2 | Solve the differential equation $(x y \sin x y+\cos x y) y d x+$ <br> $(x y \sin x y-\cos x y) x d y=0$ | Understand | 1 |
| 3 | If the air is maintained at $15^{\circ} \mathrm{C}$ and the temperature of the drops <br> from $70_{0} \mathrm{C}$ to $40^{\circ} \mathrm{C}$ in 10 minutes. What will be its temperature after <br> 30 minutes | Apply | 1 |
| 4 | If $30 \%$ of radioactive substance disappears in 10 days then how <br> long will it take for $90 \%$ of it to disappear? | Apply | 1 |
| 5 | Solve the differential equation $y\left(2 x y+e^{x}\right) d x-e^{x} d y=0$ | Understand | 1 |
| 6 | The temperature of the body drops from $100^{\circ} \mathrm{c}$ to $75^{\circ} \mathrm{c}$ in 10 minutes <br> when the surrounding air is at $20^{\circ} \mathrm{c}$. then what will be its temperature <br> after half an hour and when will be the temperature $25^{\circ} \mathrm{c}$. | Apply | 1 |
| 7 | Solve $\frac{d y}{d x}-\frac{\operatorname{tany}}{1+x}=(1+x) e^{x} \operatorname{secy}$ | Understand | 1 |
| 8 | Solve $(x+y-1) \frac{d y}{d x}=(x-y+2)$. | Understand | 1 |
| 9 | Solve $\frac{d y}{d x}+(y-1) \cos x=e^{-\sin x} \cos s^{2} x$ | Understand | 1 |
| 10 | Solve $(2 x+y-3) d y=(x+2 y-3) d x$ | Understand | 1 |

## UNIT II

Short Answer Questions

| S.No | Question | Blooms <br> taxonomy <br> level | Course <br> outcome |
| :---: | :--- | :--- | :---: |
| 1 | Solve the differential equation $\left(D^{2}-4\right) y=2 \cos ^{2} x$ | Understand | 2 |
| 2 | Solve the differential equation $\left(D^{2}+9\right)=\cos 3 x+\sin 2 x$ | Understand | 2 |
| 3 | Solve the Differential equation $\left(D^{4}+2 D^{2}+1\right) y=x^{2} \cos ^{2} x$ | Understand | 2 |
| 4 | Solve $\left(\mathrm{D}^{2}-2 \mathrm{D}+1\right) \mathrm{y}=\mathrm{x}^{2} \mathrm{e}^{3 \mathrm{x}}$ - $\sin 2 x+3$ | Understand | 2 |
| 5 | Solve the differential equation $\left(D^{2}+4\right)=\cos 2 x+\sin 3 x$ |  | 2 |
| 6 | By using variation of parameters solve $\frac{d^{2} y}{d x^{2}}+4 y=\tan 2 x$ | Understand | 2 |
| 7 | Solve the Differential Equation $\left(D^{2}+3 D+2\right) y=$ <br> $e^{2 x} \cos x+2 \cos (2 x+3)$ | Understand | 2 |
| 8 | Solve $\left(\mathrm{D}^{2}-2 \mathrm{D}+2\right) \mathrm{y}=e^{x} \tan x \quad$ by method of variation of <br> parameters | Understand | 2 |
| 9 | Solve $\left(\mathrm{D}^{2}-2 \mathrm{D}+1\right) \mathrm{y}=\mathrm{x}^{2} \mathrm{e}^{3 \mathrm{x}}-\sin 2 x+3$ | Understand | 2 |
| 10 | Solve $\left(\mathrm{D}^{2}+4 \mathrm{D}+5\right) \mathrm{y}=5$ | Understand | 2 |

Long Answer Questions

| S.No | Question | Blooms <br> taxonomy <br> level | Course <br> outcome |
| :---: | :--- | :--- | :---: |
| 1 | Solve $\frac{d^{2} y}{d x^{2}}+4 \frac{d y}{d x}+3 y=e^{-x} \operatorname{sinx}+\mathrm{x}$ | Understand | 2 |
| 2 | Solve $\frac{d^{2} y}{d x^{2}}+\frac{d y}{d x}=x^{2}+2 x+4$ | Understand | 2 |
| 3 | Solve $\frac{d^{2} y}{d x^{2}}-4 \frac{d y}{d x}+3 y=e^{x} \cos 3 x$ | Understand | 2 |
| 4 | Solve $\frac{d^{2} y}{d x^{2}}-3 \frac{d y}{d x}+2 y=x e^{3 x}+\sin 2 x$ | Understand | 2 |
| 5 | Solve $\mathrm{x}^{3} \frac{d^{3} y}{d x^{2}}+2 x^{2} \frac{d^{2} y}{d x^{2}}+2 y=10\left(x+\frac{1}{x}\right)$ | Understand | 2 |
| 6 | Solve $\left(\mathrm{D}^{2}+1\right) \mathrm{x}=\mathrm{t} \cos 2 t$ | Understand | 2 |
| 7 | Explain the method of variation of parameters. | Remember | 2 |
| 8 | Solve $\left(\mathrm{D}^{3}-3 \mathrm{D}+4\right) \mathrm{y}=0$ | Understand | 2 |
| 9 | Solve $\left(\mathrm{D}^{2}+4 \mathrm{D}+3\right) \mathrm{y}=e^{e^{x}}$ | Understand | 2 |
| 10 | Solve $\left(\mathrm{D}^{3}-6 \mathrm{D}^{2}+11 \mathrm{D}-6\right) \mathrm{y}=\mathrm{e}^{-2 \mathrm{x}}+\mathrm{e}^{-3 x}$ | Understand | 2 |

## UNIT III

## Short Answer Questions

| S.No | Question | Blooms <br> taxonomy <br> level | Course <br> outcome |
| :---: | :--- | :--- | :---: |
| 1 | Evaluate $\int_{0}^{\frac{\pi}{4}} \int_{0}^{a \sin \theta} \frac{r d r d \theta}{\sqrt{a^{2}-r^{2}}}$. | Apply | 3 |
| 2 | Change the order of integration in $\int_{0}^{1} \int_{x^{2}}^{2-x} x y d x d y$. | Apply | 3 |
| 3 | Evaluate $\int_{0}^{1} \int_{0}^{\sqrt{1-x^{2}}} \int_{0}^{\sqrt{1-x^{2}-y^{2}}} x y z d z d y d x$. | Apply | 3 |
| 4 | Evaluate $~$ <br>  <br> by the plane $x$ <br> $x$$(x+y+z) d x d y d z$ where the domain V is bounded |  |  |
| 5 | Evaluate the double integral $\int_{0}^{a} \int_{0}^{\sqrt{a^{2}-y^{2}}}\left(x^{2}+y^{2}\right) d y d x$. | Apply | 3 |
| 6 | By changing the order of integration evaluate $\int_{0}^{1} \int_{0}^{\sqrt{1-x^{2}}} y^{2} d y d x$. | Apply | 3 |
| 7 | Evaluate $\int_{0}^{\log 2} \int_{0}^{x} \int_{0}^{x+l o g y} e^{x+y+z} d z d y d x$ | Apply | 3 |
| 8 | Explain change of variable in double and triple integrals | Remember | 3 |
| 9 | Evaluate $\int_{0}^{4 a} \int_{\frac{y^{2}}{4 a}}^{x^{2} x^{2}+y^{2}} d x d y$ by change of variables in polar form | Apply | 3 |


| 10 | Sketch the region of integration of the integral <br> $\int_{0}^{2 a} \int_{\sqrt{2 a x-x^{2}}}^{\sqrt{2 a x}} f(x, y) d x d y$ | Apply | 3 |
| :---: | :--- | :---: | :---: |

## Long Answer Questions

| S.No | Question | Blooms taxonomy level | Course outcome |
| :---: | :---: | :---: | :---: |
| 1 | Evaluate $\iint_{R} y d x d y$ Where R is the region bounded by the parabolas $y^{2}=4 x$ and $x^{2}=4 y$. | Apply | 3 |
| 2 | Evaluate by changing order of integration $\int_{0}^{a} \int_{x / a}^{\sqrt{x} / a}\left(x^{2}+y^{2}\right) d x d y$ | Apply | 3 |
| 3 | Compute the value of $\iint_{R} y d x d y$ Where R is the region in the $\mathrm{I}^{\mathrm{st}}$ quadrant bounded by the Ellipse $\frac{x^{2}}{16}+\frac{y^{2}}{9}=1$. | Apply | 3 |
| 4 | Evaluate $\iiint(x+y+z) d x d y d z$ over the tetrahedron $\mathrm{x}=0$, $\mathrm{y}=0, \mathrm{z}=0$ and the plane | Apply | 3 |
| 5 | Evaluate $\iint_{R} y d x d y$ Where R is the region bounded by the parabolas $y^{2}=4 x$ and $x^{2}=4 y$. | Apply | 3 |
| 6 | Evaluate $\int_{0}^{\frac{\pi}{2}} \int_{0}^{\infty} \frac{r d r d \theta}{\left(r^{2}+a^{2}\right)^{2}}$. | Apply | 3 |
| 7 | Evaluate by changing the order of integration $\int_{0}^{1} \int_{x}^{\sqrt{2-x^{2}}} \frac{x d y d x}{\sqrt{x^{2}+y^{2}}}$ | Apply | 3 |
| 8 | Evaluate $\int_{0}^{1} \int_{0}^{1-x} \int_{0}^{1-x-y} d x d y d z$. | Apply | 3 |
| 9 | Evaluate $\int_{0}^{\pi} \int_{0}^{a(1+\cos \theta)} r^{2} \cos \theta d r d \theta$. | Apply | 3 |
| 10 | Evaluate $\int_{0}^{1} \int_{0}^{\sqrt{1-x^{2}}} y^{2} d y d x$ | Apply | 3 |

## UNIT IV

## Short Answer Questions

| S.No | Question | Blooms <br> taxonomy <br> level | Course <br> outcome |
| :---: | :--- | :--- | :---: |
| 1 | Prove that $r^{n} \bar{r}$ is Irrotational. | Understand | 4 |
| 2 | Find $\operatorname{div} \bar{f}$ where $\bar{f}=r^{n} \bar{r}$. Find $n$ if it is Solenoidal. | Understand | 4 |
| 3 | Find the directional derivative of $2 \mathrm{xy}+\mathrm{z}^{2}$ at $(1,1,3)$ in the direction <br> of i $\mathrm{i}+2 \mathrm{j}+3 \mathrm{k}$. | Understand | 4 |
| 4 | If a is constant vector prove grad(a.f $)=(\mathrm{a}$.grad) $\mathrm{f}+(\mathrm{a} \times$ curl f$)$. | Understand | 4 |
| 5 | Show that $\operatorname{curl(r^{n}\overline {r})=\overline {0}.}$ | Understand | 4 |
| 6 | Show that if $F$ and $G$ are irrotational $F X G$ is Solenoidal. | Understand | 4 |


| 7 | Find the work done by F= $(2 x-y-z) i+(x+y-z) j+(3 x-2 y-5 z) k$ <br> along a curve 'C' in the xy-plane given by $x^{2}+y^{2}=9$ | Understand | 4 |
| :---: | :--- | :---: | :---: |
| 8 | Find the work done by $\mathrm{F}=(2 \mathrm{x}-\mathrm{y}-\mathrm{z}) \mathrm{i}+(\mathrm{x}+\mathrm{y}-\mathrm{z}) \mathrm{j}+(3 \mathrm{x}-2 \mathrm{y}-5 \mathrm{z}) \mathrm{k}$ <br> along a curve 'C' in the xy-plane given by $x^{2}+y^{2}=4$ | Understand | 4 |
| 9 | If $\bar{F}=x y \bar{\imath}-z \bar{J}+x^{2} \bar{k}$ and c is the curve $\mathrm{x}=t^{2}$ | Understand | 4 |
| 10 | Evaluate the line integral $\int_{c}\left[\left(x^{2}+x y\right) d x+\left(x^{2}+y^{2}\right) d y\right]$ where c <br> is the square formed by the lines $x \pm 1$ | Apply | 4 |

## Long Answer Questions

| S.No | Question | Blooms taxonomy level | Course outcome |
| :---: | :---: | :---: | :---: |
| 1 | Prove that $\nabla\left(r^{n}\right)=n r^{n-2} \bar{r}$. | Understand | 4 |
| 2 | Prove that $\operatorname{div}(\bar{a} \times \bar{b})=\bar{b} . \operatorname{curl} \bar{a}-\bar{a} . \operatorname{curl} \bar{b}$ | Understand | 4 |
| 3 | (a) Prove that $\left(\operatorname{grad} r^{m}\right)=m(m+1) r^{m-2}$. <br> (b) Show that curl $(\operatorname{curl} F)=\operatorname{grad}(\operatorname{div} F)-\nabla^{2} F$. | Understand | 4 |
| 4 | S.T $\nabla \times(\nabla \times \overline{\mathrm{a}})=\nabla(\nabla . \overline{\mathrm{a}})-\nabla^{2} \overline{\mathrm{a}}$. | Understand | 4 |
| 5 | If $\bar{r}$ is the position vector of the point $\mathrm{P}(\mathrm{x}, \mathrm{y}, \mathrm{z})$ then P.T $\nabla \mathrm{f}(r)=$ $f^{I}(r) \frac{\bar{r}}{r}$. | Understand | 4 |
| 6 | Find the value of a and b so that the surfaces $\mathrm{a} x^{2}-b y z=(a+2) x$ and $4 x^{2} y+z^{3}=4$ may intersect orthogonally at the point $(1,-1$, $2)$. | Understand | 4 |
| 7 | Find the angle between the surfaces $x^{2}+y^{2}+z^{2}=9$ and $z=$ $x^{2}+y^{2}-3$ at the point $(2,-1,2)$. | Understand | 4 |
| 8 | S.T $\nabla^{2}[f(r)]=\frac{d^{2} f}{d r^{2}}+\frac{2}{r} \frac{d f}{d r}$. Where $\mathrm{r}=\|\bar{r}\|$. | Understand | 4 |
| 9 | P.T $\nabla \times\left(\frac{\bar{A} \times \bar{r}}{r^{n}}\right)=\frac{(2-n) \bar{A}}{r^{n}}+\frac{n(\bar{r} \cdot \bar{A}) \bar{r}}{r^{n+2}}$ | Understand | 4 |
| 10 | P.T $\operatorname{Curl}(\bar{a} \times \bar{b})=\bar{a} \operatorname{div} \bar{b}-\bar{b} \operatorname{div} \bar{a}+(\bar{b} . \nabla) \bar{a}-(\bar{a} . \nabla) \bar{b}$. | Understand | 4 |

## UNIT V

## Short Answer Questions

| S.No | Question | Blooms <br> taxonomy <br> level | Course <br> outcome |
| :---: | :--- | :--- | :---: |
| 1 | State Gauss divergence theorem. | Remember | 5 |
| 2 | State Green's theorem in a plane, | Remember | 5 |
| 3 | State Stoke's theorem. | Rember | 5 |
| 4 | Verify Green's theorem in plane for $\oint\left(3 x^{2}-8 y^{2}\right) d x+$ <br> $(4 y-6 x y) d y$ where $C$ is the region bounded by $y=\sqrt{x}$ and $y=$ <br> $x^{2}$. | 5 |  |
| 5 | Evaluate $\iint_{S} \bar{F} \cdot \bar{n} d s$, where $\bar{F}=2 x^{2} y \bar{\imath}-y^{2} \bar{J}+4 x z^{2} \bar{k}$ and $S$ is the <br> closed surface of the region in the first octant bounded by the <br> cylinder $y^{2}+z^{2}=9$ and the planes $x=0, x=2, y=0, z=0$. | Apply | 5 |


| 6 | Verify Stokes theorem for $\bar{F}=(y-z+2) \bar{\imath}+(y z+4) \bar{\jmath}-x z \bar{k}$ <br> where $S$ is the surface of the cube $x=0, y=0, z=0, x=2, y=$ <br> $2, z=2$ above the $x y$-plane. | Apply | 5 |
| :---: | :--- | :--- | :---: |
| 7 | Apply stokes theorem, to evaluate $\left.\oint_{c} y d x+z d y+x d z\right)$ where c is <br> the curve of intersection of the sphere $x^{2}+y^{2}+z^{2}=a^{2}$ and $x+$ <br> $z=a$ | Apply | 5 |
| 8 | Apply stoke's theorem and show that $\iint_{S} c u r l \bar{F} . \bar{n} d s=$ <br> $0 w h e r e \bar{F}$ is any vector and s=x $+y^{2}+z^{2}=1$ | Apply | 5 |
| 9 | Verify green's theorem in the plane for $\oint_{c}\left(x^{2}-x y^{3}\right) d x+$ <br> $\left(y^{2}-2 x y\right) d y$ where C is a Square with vertices <br> $(0,0),(2,0),(2,2),(0,2)$ | Apply | 5 |
| 10 | Apply Green'stheorem to Evaluate $\oint_{c}\left(2 x^{2}-y^{2}\right) d x+\left(x^{2}+y^{2}\right) d y$ <br> where c is the boundary of the area enclosed by the x-axis and upper <br> half of the circle $x^{2}+y^{2}=a^{2}$ | Apply | 5 |

## Long Answer Questions

| S.No | Question | Blooms taxonomy level | Course outcome |
| :---: | :---: | :---: | :---: |
| 1 | Verify Gauss Divergence Theorem for $\bar{f}=\left(x^{3}-y z\right) \bar{\imath}-$ $2 x^{2} y \bar{\jmath}+z \bar{k}$ taken over the surface of the cube bounded by the planes $\mathrm{x}=\mathrm{y}=\mathrm{z}=\mathrm{a}$ and coordinate planes . | Apply | 5 |
| 2 | If $\bar{F}=4 x z \bar{\imath}-y^{2} \bar{\jmath}+y z \bar{k}$ evaluate $\int_{S} \bar{F} \cdot \bar{n} d s$ where $S$ is the surface of the cube bounded by $x=0, x=a, y=0, y=a, z=0, z=a$. | Apply | 5 |
| 3 | Verify Green's theorem in plane for $\oint\left(3 x^{2}-8 y^{2}\right) d x+$ $(4 y-6 x y) d y$ where $C$ is the region bounded by $y=\sqrt{x}$ and $y=$ $x^{2}$. | Apply | 5 |
| 4 | Evaluate $\iint_{S} \bar{F} . \bar{n} d s$, where $\bar{F}=2 x^{2} y \bar{\imath}-y^{2} \bar{J}+4 x z^{2} \bar{k}$ and $S$ is the closed surface of the region in the first octant bounded by the cylinder $y^{2}+z^{2}=9$ and the planes $x=0, x=2, y=0, z=0$. | Apply | 5 |
| 5 | Verify Stokes theorem for $\bar{F}=(y-z+2) \bar{\imath}+(y z+4) \bar{\jmath}-x z \bar{k}$ where $S$ is the surface of the cube $x=0, y=0, z=0, x=2, y=$ $2, z=2$ above the $x y$-plane. | Apply | 5 |
| 6 | Evaluate $\iiint \nabla \cdot F d V$ where V is the cylindrical region bounded by $\mathrm{x}^{2}$ $+y^{2}=9, z=0, z=2, F=y i+x j+z^{2} k$. | Apply | 5 |
| 7 | Verify Green's Theorem in a plane for $\int_{C}(y-\sin x) d x+\cos x d y$ where C is the triangle joins $(0,0),(\pi /, 0),(\pi / 2,1)$. | Apply | 5 |
| 8 | Evaluate using Green's theorem $\int_{C} x 2 y d x+y 3 d y$ where C is the closed path formed by $\mathrm{y}=\mathrm{x}, \mathrm{y}^{3}=\mathrm{x}^{2}$ form $(0,0)$ to $(1,1)$. | Apply | 5 |
| 9 | Evaluate $\iint \mathrm{F} \cdot n d S$ where $F=\mathrm{xzi}+\mathrm{yzj}+\mathrm{z}^{2} \mathrm{k}$ and S is the upper half of the sphere $x^{2}+y^{2}+z^{2}=1$. | Apply | 5 |
| 10 | Use divergence theorem to Evaluate $\iint\left(y^{2} z^{2} i+z^{2} x^{2} j+z^{2} y^{2} k\right) . n$ ds where S is the part of the unit sphere above the $\mathrm{x} y$ plan. | Apply | 5 |

## OBJECTIVE QUESTIONS: JNTUH

## UNIT I

1.The general solution of $\frac{d y}{d x}=e^{x+y}$
a) $e^{x}+e^{y}=\mathrm{c}$
b) $e^{x}-e^{y}=\mathrm{c}$
c
$e^{x y}=\mathrm{c}$
d) none
2. The integrating factor of $\left(x^{3} y^{3}+x^{2} y^{2}+x y\right) y d x+\left(x^{3} y^{3}-x^{2} y^{2}-x y\right) x d y=0$
a) $\frac{1}{2 \mathbf{x y}(1+\mathbf{x y})}$
b) $\frac{1}{2 \mathbf{x}^{2} \mathbf{y}^{2}(1+\mathbf{x y})}$
c) $\frac{1}{1+x y}$
d) none
3. Degree of $\frac{\mathbf{d}^{2} \mathbf{y}}{\mathbf{d x}^{2}}-2 \frac{\mathbf{d y}}{\mathbf{d x}}+10 \mathbf{y}=0$ is
a) 0
b) 1
c) 2
d) none
4. The condition for exactness of differential equation if $\mathrm{M} d x+\mathrm{N} d y=0$ is
a) $\frac{\partial \mathbf{M}}{\partial \mathbf{x}}=\frac{\partial \mathbf{N}}{\partial \mathbf{y}}$
b) $\frac{\partial \mathbf{M}}{\partial \mathbf{y}}=\frac{\partial \mathbf{N}}{\partial \mathbf{x}}$
c) $\frac{-\partial \mathbf{M}}{\partial \mathbf{x}}=\frac{\partial \mathbf{N}}{\partial \mathbf{y}}$
d) none
5. Evaluate the Wronskian of $e^{x} \& x$ is $\qquad$
a) $(1-x) e^{x}$
b) $(x+1) e^{x}$
c) $x e^{x}$
d) none
6. P.I. of $\frac{d^{3} y}{d x^{3}}+y=e^{-x}$ is
a) $x e^{\frac{-x}{3}}$
b) $e^{\frac{-x}{3}}$
c) $-x e^{\frac{-x}{3}}$
d) none
7. The order of $\frac{\mathbf{d}^{2} \mathbf{y}}{\mathbf{d x}^{2}}-2 \frac{\mathbf{d y}}{\mathbf{d x}}+10 \mathbf{y}=0$ is
a) 0
b) 1
c) 2
d) none
8) The general solution of $\frac{y d x-x d y}{y^{2}}=0$
a) $x y=\mathrm{c}$
b) $x=\mathrm{c} y$
c) $y=\mathrm{c} x$
d) none
9) The equation $\frac{d y}{d x}+\frac{a x+h y+g}{h x+b y+f}=0$ is $\qquad$
a) homogeneous
b) non- homogeneous
c) exact
d) none
10) The general solution of $\frac{x d y+y d x}{y^{2}+x^{2}}=0$
a) $\log (x+y)=\mathrm{c}$
b) $\log \left(x^{2}+y^{2}\right)=c$
c) $\log x y=\mathrm{c}$
d) none
11. The order and degree of $\frac{d^{2} y}{d y^{2}}=\left[y+\left(\frac{d y}{d x}\right)^{6}\right]^{1 / 4}$ is $\qquad$

12 If $x \frac{d y}{d x}=x^{2}+y-2, y(1)=1$ then $\mathrm{y}(2)=$ $\qquad$
13. The general solution of linear differential equation $\frac{d y}{d x}=e^{x+y}$ is $\qquad$
14. The differential equation is said to be homogeneous if $\qquad$
15. The order of the differential equation $x^{3} \frac{d^{3} y}{d x^{3}}+2 x^{2} \frac{d^{2} y}{d x^{2}}-3 y=x$ is $\qquad$
16. Newton's law of cooling is $\qquad$
17. The general solution of $\mathrm{p}^{2}-5 \mathrm{p}-6=0$ where $\mathrm{p}=\frac{d y}{d x}$ is $\qquad$
18. The general solution of linear differential equation is $\qquad$
19. The solution of $\sqrt{ } 1+x^{2} d y+\sqrt{ } 1+y^{2} d x=0$ is $\qquad$
20. The solution of $\frac{d y}{d x}+y \tan x=y^{2} \sec x$ is $\qquad$

## UNIT II

1. The general solution of $\frac{\mathbf{d}^{2} \mathbf{y}}{\mathbf{d x}^{2}}-2 \frac{\mathbf{d y}}{\mathbf{d x}}+10 \mathbf{y}=0$ is
a) $y=e^{x}\left(C_{1} \operatorname{Cos} 3 x+C_{2} \operatorname{Sin} 3 x\right)$
b) $y=C_{1} \operatorname{Cos} 3 x+C_{2} \operatorname{Sin} 3 x$
c) $y=C_{1} e^{3 x}+C_{2} e^{-3 x}$
d) none
2. $\frac{1}{(\mathbf{D}-2)^{2}} \mathbf{e}^{2 \mathrm{x}} \sin \mathbf{x}=$
a) $e^{2 x} \sin x$
b) $-e^{2 x} \sin x$
c) $\mathrm{e}^{2 x} \frac{\mathbf{x}^{2}}{2} \sin 2 \mathbf{x}$
d) none
3. $x^{2} \frac{d^{2} y}{d x^{2}}+4 x \frac{d y}{d x}+2 y=e^{x}$ is known as $\qquad$ .
a) Cauchy Euler equation
b) Legender equation
c) Homogeneous equation
d) none
4. P.I. of $(D-1)^{4} y=e^{x}$ is
a) $\frac{x^{4}}{4} e^{x}$
b) $x^{4} e^{x}$
c) $e^{x}$
d) $e^{x} / 4$
5. P.I. of $\left(D^{2}-2 D+1\right) y=\operatorname{Coshx}$ is
a) $\frac{x^{2}}{4} e^{x}+\frac{e^{-x}}{8}$
b) $\frac{x^{2}}{4} e^{-x}+\frac{e^{x}}{8}$
c) $\frac{x^{2}}{4} e^{x}$
d) $c_{1} e^{x}+c_{2} e^{-x}$
6. Complementary Function of $(D-1)^{4} y=e^{x}$ is
a) $\frac{x^{4}}{4} e^{x}$
b) $x^{4} e^{x}$
c) $\left(c_{1}+c_{2} x+c_{3} x^{2}+c_{4} x^{3}\right) e^{x}$
d) $e^{x / 4}$
7. Complementary Function of $\left(D^{2}-2 D+1\right) y=C o s h x$ is
a) $\frac{x^{2}}{4} e^{x}+\frac{e^{-x}}{8}$
b) $\left(c_{1}+c_{2} x\right) e^{x}$
c) $\frac{x^{2}}{4} e^{x}$
d) $c_{1} e^{x}+c_{2} e^{-x}$
8. General solution of $\left(D^{2}+1\right) y=0$ is
a) $c_{1} \cos x+c_{2} \sin x$
b) $\frac{x^{2}}{4} e^{-x}+\frac{e^{x}}{8}$
c) $\frac{x^{2}}{4} e^{x}$
d) $c_{1} e^{x}+c_{2} e^{-x}$
9). $\frac{\sin x}{D^{2}+D+1}=$
a) $\sin x$
b) $\cos x$
c) $\frac{\sin x}{3}$
d) none
10) P.I. of $\left(D^{2}+a^{2}\right) y=C o s a x$ is
a) $x \cos a x$
b) $x \sin a x$
c) $\frac{x \sin a x}{2 a}$
d) none
11. The Integrating factor of $\frac{d y}{d x}+\mathrm{p}(\mathrm{x}) \mathrm{y}=\mathrm{q}(\mathrm{x})$ is $\qquad$
12. $\qquad$ is the particular integral of $\left(D^{2}+5 D+6\right) y=e^{x}$
13. The integrating factor of $\left(1-x^{2}\right) y+x y=a x$ is $\qquad$
14. The complementary function of $(D-1)^{2} y=\sin 2 x$ is $\qquad$
15. The value of $\frac{1}{D+2}\left(x+e^{x}\right)$ is $\qquad$
16. The solution of the Differential equation $\left(D^{2}+4\right) y=\tan 2 x$ is $\qquad$
17. The particular integral of $\left(D^{2}+a^{2}\right) y=\operatorname{cosa} x$ is $\qquad$
18. The solution of the Differential equation $\left(D^{2}+4\right) y=\sec 2 x$ is $\qquad$
19. The value of $\frac{1}{D^{2}+D+1} \sin x$ is $\qquad$
20. The solution of $\left(D^{2}-4 D+4\right) y=x^{2} \sin x+e^{2 x}+3$ is $\qquad$

## UNIT III

1. $\int_{0}^{1} \int_{0}^{2} \int_{0}^{2} x^{2} y z d z d y d x=$ $\qquad$ —.
a) $1 / 2$
b) $1 / 4$
c) 1
d) $3 / 2$
2. $\int_{0}^{1} \int_{1}^{2} x y d y d x=$ $\qquad$
a) $1 / 2$
b) $1 / 4$
c) 1
d) $3 / 4$
3. $\int_{0}^{\pi} \int_{0}^{a \cos \theta} r \sin \theta d r d \theta=$ $\qquad$
a) $\frac{a^{2}}{2}$
b) $\frac{a^{2}}{3}$
c) $\frac{a^{3}}{4}$
d) $\frac{a^{3}}{3}$
4. The volume of the tetrahedron bounded by the coordinate planes and the plane

$$
x+y+z=1 \text { is }
$$

$\qquad$ .
a) $\frac{1}{2}$
b) $\frac{1}{3}$
c) $\frac{1}{4}$
d) $\frac{1}{6}$
5. The volume of the tetrahedron bounded by the surfaces $x=0, y=0, z=0$ and $\frac{x}{a}+\frac{y}{b}+\frac{z}{c} 1$ is $\qquad$ -.
a) $\frac{a b c}{2}$
b) $\frac{a b c}{3}$
c) $\frac{a b c}{4}$
d) $\frac{a b c}{6}$
6. In polar coordinates $\int_{0}^{\infty} \int_{0}^{\infty} e^{-\left(x^{2}+y^{2}\right)} d x d y=$ $\qquad$ -.
a) $\int_{0}^{\frac{\pi}{2}} \int_{0}^{\infty} e^{-r^{2}} d r d \theta$
b) $\int_{0}^{\frac{\pi}{4}} \int_{0}^{\infty} e^{-r} r d r d \theta$
c) $\int_{0}^{\frac{\pi}{2}} \int_{0}^{\infty} e^{-r^{2}} r d r d \theta$
d) $\int_{0}^{\frac{\pi}{2}} \int_{0}^{\infty} e^{-r} d r d \theta$
7. An equivalent iterated integral with order of integration reversed for $\int_{0}^{1} \int_{1}^{\mathrm{X}} \mathrm{dy} d \mathrm{~d}$ is $\qquad$ -
a) $\int_{0}^{1} \int_{1}^{e^{y}} d x d y$
b) $\int_{1}^{e} \int_{\log y}^{1} d x d y$
c) $\int_{\text {e }}^{1} \int_{1}^{\log y} d x d y$
d) none.
8. The integrated integral for $\int_{-1}^{1} \int_{0}^{\sqrt{1-x^{2}}} f(x, y) d y d x$ after changing order of integration is
a) $\int_{-1}^{1} \int_{\sqrt{1-y^{2}}}^{\sqrt{1-y^{2}}} f d x d y$
b) $\int_{-1}^{1} \int_{0}^{\sqrt{1-x^{2}}} f d x d y$
c) $\int_{0}^{1} \int_{\sqrt{1-y^{2}}}^{\sqrt{1-y^{2}}} f d x d y$
d) none
9. $\iiint\left(x^{2}+y^{2}+z^{2}\right) d z d y d x$ where $v$ is the volume of the cube bounded by the coordinate planes $x=y=z=9$ is $\qquad$ .
a) $a^{5} / 5$
b) $a^{5} / 25$
c) $a^{5}$
d) $(0.2 \mathrm{a})^{5}$
10. The volume of the solid generated by revolution of part of the parabola $y^{2}=4 a x$ cut off by latus rectum about the tangent at the vertex is $\qquad$ .
a) $\frac{8 \pi a^{3}}{5}$
b) $\frac{16 \pi a^{3}}{5}$
c) $\frac{4 \pi a^{3}}{5}$
d) $\frac{2 \pi a^{3}}{5}$
11. The area of the portion of the plane $x+y+z=1$ in the first octant is $\qquad$ .
12. The value of $\iint x y d x d y$ over the area bounded by parabola $\mathrm{x}=2 \mathrm{a}$ and $\mathrm{x}^{2}=4 \mathrm{ay}$ is $\qquad$ .
13. $\int_{0}^{2} \int_{0}^{x}(x+y) d y d x=$ $\qquad$ .
14. What is the volume bounded by $\mathrm{z}=x^{2}+y^{2}$ and $\mathrm{z}=4$ $\qquad$ .
15. $\int_{-1}^{1} \int_{-2}^{2} \int_{-3}^{3} d z d y d x$ is $\qquad$ .
16. The iterated integral for $\int_{-1}^{1} \int_{0}^{x} f(x, y) d y d x$ after changing the order of integration is _
17. $\int_{0}^{\pi} \int_{0}^{a \cos \theta} r d r d \theta$ is $\qquad$ .
18. The value of $\iiint(x+y+z) d x d y d z$ over the tetrahedron bounded by the co-ordinate planes and the plane $\mathrm{x}+\mathrm{y}+\mathrm{z}=1$ is $\qquad$ .
19. The relation between the Cartesian coordinates $x, y, z$ and the Cylindrical coordinates $\rho, \theta, z$ is $\qquad$ .
20. The value of volume bounded the $y z$ plane, the cylinder $y^{2}+z^{2}=4$ and the plane $x+y+z=3$ is $\qquad$ _.

## UNIT IV

1. If $\bar{r}$ is the position vector of any point in space, then $\mathrm{r}^{\mathrm{n}} \bar{r}$ is $\qquad$ _.
a) Irrotational
b) Solenoidal
c) $\operatorname{both}(\mathrm{a} \& b)$
d) none
2. If curl $\bar{r}=0$ then $\bar{r}$ is $\qquad$ .
a) Solenoidal
b) Irrotational
c) $\operatorname{both}(a \& b)$
d) none
3. If curl $(\operatorname{grad} \phi)=0$ then $\operatorname{grad} \phi$ is $\qquad$ .
a) Solenoidal
b) both(a\&c)
c) Irrotational
d)none
4. If div $\bar{f}=0$ then $\bar{f}$ is $\qquad$ .
a) Solenoidal
b) Irrotational
c) both
d)none
5. If $\bar{a}$ is const vector then $\operatorname{grad}(\bar{a} \cdot \bar{r})$ is $\qquad$ .
a) $\bar{a}$
b) 0
c) 1
d) none
6. $f=x^{3}+y^{3}+3 x y z$ then $\operatorname{grad} f=$ $\qquad$ .
a) $-\left(3 \mathrm{x}^{2}+3 \mathrm{yz}\right) \bar{i}+\left(3 \mathrm{y}^{2}+3 \mathrm{xy}\right) \bar{j}+3 \mathrm{xy}$
b) $\left(3 \mathrm{x}^{2}+3 \mathrm{yz}\right) \bar{i}+\left(3 \mathrm{y}^{2}+3 \mathrm{xy}\right) \bar{j}+3 \mathrm{xy}$
c) 0
d) none
7. If $\bar{r}=\mathrm{xi}+\mathrm{yj}+\mathrm{zk}$ then $\nabla \cdot\left[\bar{r} / \mathrm{r}^{3}\right]=$ $\qquad$ .
a) 1
b) 0
c) -1
d) none
8. $\bar{r}=x i+y j+z k$ then $\nabla[f(r)]=$ $\qquad$ .
a) $\mathrm{f}^{1}(\mathrm{r}) / \mathrm{r}$
b) $\bar{r} \mathrm{f}^{1}(\mathrm{r}) / \mathrm{r}$
c) $\bar{r} \mathrm{f}^{1}(\mathrm{r})$
d)none
9. If $\bar{r}=x i+y j+z k$ then $\operatorname{grad}\left(\mathrm{r}^{\mathrm{n}}\right)$ is $\qquad$ .
a) $\mathrm{nr}^{\mathrm{n}-2} \bar{r}$
b) $\mathrm{r}^{\mathrm{n}-2} \bar{r}$
c) 0
d)none
10. $\nabla[\nabla \cdot \bar{r} / \mathrm{r}]=$ $\qquad$ .
a) $2 \bar{r} / \mathrm{r}^{3}$
b) $-2 \bar{r} / \mathrm{r}^{3}$
c) $\bar{r} / \mathrm{r}^{3}$
d)none
11. $\nabla\left[\mathrm{r} \nabla\left(1 / \mathrm{r}^{3}\right)\right]=$ $\qquad$
12. If $\emptyset=x^{2}+y^{2}+z^{2}-3 x y z$ then $\operatorname{curl}(\operatorname{grad} \emptyset)=$ $\qquad$
13. If $\bar{r}=x i+y j+z k$ then $\nabla^{2}\left(\frac{1}{\mathrm{r}}\right)=$ $\qquad$
14. If $\bar{r}=\mathrm{xi}+\mathrm{yj}+\mathrm{zk}$ and if $\left(\mathrm{r}^{\mathrm{n}} \bar{r}\right)$ is solenoidal then $n=$ $\qquad$
15. If $\bar{a}$ is const vector then $\operatorname{curl}(\bar{r} \times \bar{a})$ is $\qquad$
16. If $\emptyset=a x^{2}+b y^{2}+c z^{2}$ satisfies Laplacian equation then $a+b+c=$ $\qquad$
17. If curl $\bar{a}=0$ then $\bar{a}$ is called
18. Physical interpretation of $|\boldsymbol{\nabla} \varphi|$ is $\qquad$
19. Laplacian operator is denoted by $\qquad$
20. The harmonic function of $\varphi$ is $\qquad$

## UNIT V

1. The work done by the force $(3 x-2 y) i+(y+2 z) j-\left(x^{2}\right) k$ in moving along the straight line joining $(0,0,0) \&(1,1,1)$ is $\qquad$ .
a) $1 / 2$
b) $2 / 5$
c) $5 / 3$
d) none
2. The circulation of $\bar{F}=(2 \mathrm{x}-\mathrm{y}+2 \mathrm{z}) \mathrm{i}+(\mathrm{x}+\mathrm{y}-\mathrm{z}) \mathrm{j}+(3 \mathrm{x}-2 \mathrm{y}-5 \mathrm{z}) \mathrm{k}$ along the circle $\mathrm{x}^{2}+\mathrm{y}^{2}=4$ in the xy plane is $\qquad$ -.
a) $8 \pi$
b) $5 \pi$
c) $3 \pi$
d) none
3. If $\bar{F}=\left(x+y^{2}\right) \mathrm{i}-2 \mathrm{xj}+2 \mathrm{yzk}$ evaluate $\int \bar{F} \cdot \bar{n}$ ds over the surface $\mathrm{x}^{2}+\mathrm{y}^{2}+\mathrm{z}^{2}=1$ in the first octant is $\qquad$ .
a) $2 / 8$
b) $3 / 8$
c) $1 / 8$
d) none
4. If any closed surface S enclosing a volume V and $\bar{F}=\mathrm{xi}+2 \mathrm{yj}+3 \mathrm{zk}$ then $\iint \bar{f} \cdot \bar{n} \mathrm{ds}=$
$\qquad$ .
a) 6 V
b) 5 V
c) 2 V
d) none
5. $\iint(x d y d x+y d z d x+z d x d y)$ where surface $\mathrm{x}^{2}+\mathrm{y}^{2}+\mathrm{z}^{2}=\mathrm{a}^{2}$ is $\qquad$ .
a)
b)
c) $4 \pi a^{3}$
d) none
6. $\oint M d x+N d y=$ $\qquad$ .
a) $\oiint_{S}\left(\frac{\partial N}{\partial x}+\frac{\partial M}{\partial y}\right) d x d y$
b) $\oiint_{S}\left(\frac{\partial N}{\partial x}-\frac{\partial M}{\partial y}\right) d x d y$
c) 0
d) none
7. If $\bar{F}=\left(\mathrm{x}^{2}+\mathrm{y}^{2}\right) \mathrm{i}-2 \mathrm{xj}+2 \mathrm{yzk}$ evaluate $\int \bar{F} \cdot \bar{n}$ ds over the surface $\mathrm{x}^{2}+\mathrm{y}^{2}+\mathrm{z}^{2}=1$ in the first octant is- $\qquad$ .
a) $3 / 8$
b) $1 / 2$
c) $3 / 4$
d) none
8. The necessary and sufficient condition that the line integral $\int A . \mathrm{dr}=0$ for every closed curve C is $\qquad$ .
a) simple
b) multiple
c) both
d) none
9. The volume of the line integral $\int \operatorname{grad}(x+y-z) d$ from $(0,1,-1)$ to $(1,2,0)$ is
$\qquad$ .
a) -3
b) 3
c) 0
d) none
10. If $\bar{F}=$ axi-byj+czk then $\iint \bar{f} . \bar{n}$ ds where $S$ is the surface of the unit sphere is $\qquad$ .
a) $\frac{4}{3} \pi(a+b+c)$.
b) $-\frac{4}{3} \pi(a+b+c)$.
c) $\frac{4}{3} \pi(a-b+c)$.
d)none
11. A conservative force field is $\qquad$
12. The relation between surface and volume integrals represents $\qquad$ theorem
13. If $\bar{n}$ is the unit outward drawn normal to any closed surface then $\int \operatorname{div} \bar{n} \mathrm{dV}$ is $\qquad$
14. The representation of line integral is $\qquad$
15. The value of $\int[(x 2+x y) d x+(x 2+y 2) d y]$ over the region $\mathrm{x}=0, \mathrm{x}=1, \mathrm{y}=0, \mathrm{y}=1$ is $\qquad$ .
16. The representation of volume integral is $\qquad$
17. The relation between line and surface integrals represents $\qquad$ theorem
18. The value of $\int\left[e^{x} d x+2 y d y-d z\right]$ over the region $x^{2}+y^{2}=9, z=2$ is $\qquad$ .
19. The representation of surface integral is $\qquad$
20. The relation between line and double integrals represents $\qquad$ theorem

## WEBSITES:

1. www.geocities.com/siliconvalley/2151/matrices.html
2. www.mathforum.org/key/nucalc/fourier.html
3. www.mathworld.wolfram.com
4. www.eduinstitutions.com/rec.htm
5. www.isical.ac.in
6. http://nptel.ac.in/courses/111108066/
7. http://nptel.ac.in/courses/111106051/
8. http://nptel.ac.in/courses/111102011/
9. http://nptel.ac.in/syllabus/syllabus.php?subjectId=111103019

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## JOURNALS:

## INTERNATIONAL

1. Journal of American Mathematical Society
2. Journal of differential equations - Elsevier
3. Pacific Journal of Mathematics
4. Journal of Australian Society
5. Bulletin of "The American Mathematical Society"
6. Bulletin of "The Australian Mathematical Society"
7. Bulletin of "The London Mathematical Society"

NATIONAL

1. Journal of Interdisciplinary Mathematics
2. Indian Journal of Pure and Applied Mathematics
3. Indian Journal of Mathematics
4. Proceedings of Mathematical Sciences
5. Journal of Mathematical and Physical Sciences.
6. Journal of Indian Academy and Sciences

## LIST OF TOPICS FOR STUDENT SEMINARS:

1. Orthogonal trajectory.
2. Natural law of growth and decay.
3. Newton's law of cooling.
4. Evaluation of Multiple integration.
5. Geometrical interpretation of Curl and Divergence.

## CASE STUDIES / SMALL PROJECTS:

1. Describe about the Quadratic forms and its nature.
2. Discuss about the Concept of simple harmonic motion and electrical circuits in detail.
3. Describe about the geometrical meaning of double and triple integration.
4. Discuss about the orthogonal trajectory with examples.
5. Discuss the applicability of vector integral theorem.

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